## A Review of Recent Research on Nanoindentation of High-Entropy Alloys Processed by High-Pressure Torsion

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High entropy alloys (HEAs) are a novel class of materials that have emerged as potential candidates for various industrial applications due to their excellent mechanical properties at cryogenic, ambient, elevated temperatures, and even under a hydrogen environment. The incorporation of nanocrystalline (nc) structure into HEAs has attracted significant attention for the further enhancement of their exceptional properties, as exceptional grain refinement usually results in enhanced strength without a large expense of ductility. High-pressure torsion (HPT) is often considered one of the most efficient methods for nanocrystallization, and this also holds true for HEAs. Recently, nanoindentation technique has been widely utilized to explore the relationship between HPT-induced grain refinement and mechanical behavior due to the inhomogeneous microstructure within the HPT disk. In this report, recent nanoindentation studies performed on HPT-processed HEAs are comprehensively reviewed with special emphasis on the nanomechanical behavior of nc HEAs. [doi:10.2320/matertrans.MT-MF2022015]

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#### 1. Introduction

High entropy alloys (HEAs) are a new member of structural materials introduced in 2004,1,2) which were defined originally as alloys consisting of at least five principal elements in (near-)equiatomic compositions. Recently, the concept of HEAs has been extended to an alloy with 2 to 4 principal elements, which is usually referred to as medium-entropy alloys (MEAs) having configurational entropy in the range of 0.69R-1.61R (where R is the molar gas constant).<sup>3–5)</sup> Due to the relatively high configurational entropy, M/HEAs often exhibit a simple solid solution phase having body-centered cubic (BCC),<sup>6,7)</sup> face-centered cubic (FCC)<sup>8,9)</sup> or hexagonal close-packed (HCP) structures.<sup>10,11)</sup> M/HEAs possess (1) an outstanding combination of strength and ductility,<sup>12-14)</sup> (2) high resistance to corrosion,<sup>15,16)</sup> hydrogen embrittlement,<sup>17,18</sup>) wear,<sup>19,20</sup> and fatigue,<sup>21,22</sup>) and (3) excellent strength retention at cryogenic and elevated temperatures.<sup>9,23-25)</sup> These exceptional properties of M/ HEAs could be further improved by tailoring the microstructure (e.g., introducing multiple phases, 26,27) short-range ordering,  $^{28-30)}$  or refined microstructure  $^{31-33)}$ ).

Since the grain boundaries (GBs) are a representative example of the defects controllable in an easy and obvious manner, grain refinement might be the most effective way to improve the mechanical strength according to the so-called Hall-Petch relation:<sup>34,35</sup>)

$$\sigma = \sigma_0 + k_{HP} d^{-0.5} \tag{1}$$

where  $\sigma$  is the strength for either yielding  $(\sigma_y)$  or plastic flow  $(\sigma_f)$ ,  $\sigma_0$  is the friction stress that is free from GB

contributions, *d* is grain size, and  $k_{\rm HP}$  is a material constant that is often referred to as the locking parameter or Hall–Petch coefficient. In addition, considering that the  $k_{\rm HP}$  value of HEAs, particularly for the FCC structured ones, was found to be significantly higher than for the conventional FCC metals, reducing *d* to below ~100 nm, i.e., within the nanocrystalline (nc) regime, this appears to be a promising approach for strengthening M/HEAs.<sup>31,32,36,37)</sup>

At present, the application of severe plastic deformation (SPD) is known as the most effective 'top-down' strategy to achieve exceptional grain refinement in bulk coarse-grained (cg) materials.<sup>38–40)</sup> Although there are several conventional methods such as intensive rolling, fast forging, and shot peening for inducing high strain, the most known SPD processes that have received the most scientific and industrial attention include equal-channel angular pressing (ECAP),<sup>41)</sup> high-pressure torsion (HPT),42) and accumulative rollbonding (ARB).43) This is primarily because the level of applied strain upon ECAP, HPT, and ARB can be continuously increased by repeating the procedure without considerably changing the overall dimensions of the workpieces. Compared with ECAP and ARB, HPT processing has the advantage of introducing higher accumulative strains and thus leading to an exceptional level of grain refinement.<sup>39,44-50)</sup> In fact, it was demonstrated that for several HEAs, the nc structure could be achieved from the very early stage of HPT, establishing the HPT processing as the most efficient way for exploiting the synergy between HEA and nc alloys.<sup>31,32,36,37)</sup> As a result, HPT processing has been used for improving the mechanical properties several M/HEAs, such as CoCrFeMnNi,<sup>31,36)</sup> of CoCrFeNi,<sup>51,52)</sup> Al<sub>0.3</sub>CoCrFeNi,<sup>32,53)</sup> Al<sub>0.5</sub>CoCrFeMnNi,<sup>54)</sup> AlCrFeCoNiNb,<sup>55)</sup> TiZrNbHfTa,<sup>37,56)</sup> AlFeCoNiCu,57) CrFe<sub>2</sub>NiMnV<sub>0.25</sub>,<sup>58)</sup> TiZrCrMnFeNi,<sup>59)</sup> AlTiFeCoNi,<sup>60)</sup> AlTiFeCoNi-C<sup>61)</sup> and CoCrFeMnNi-C.<sup>62)</sup> More recently,

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the application of HPT has been extended to nonmetallic high-entropy materials, including high-entropy hydride MgTiVCrFe–H,<sup>63)</sup> high-entropy oxide TiZrHfNbTaO<sub>11</sub>,<sup>64)</sup> and high-entropy oxynitride TiZrHfNbTaO<sub>6</sub>N<sub>3</sub><sup>65)</sup> for investigating their potential applications in hydrogen-related industries. It is noteworthy that the hardness value of AlCrFeCoNiNb HEA increases to ~1030 HV (or ~10.9 GPa) after HPT-processing,<sup>55)</sup> which represents the highest hardness value reported among the aforementioned HEAs.

The equivalent strain imposed by the HPT process is inhomogeneously distributed across the HPT disk (which has generally a diameter of 10 mm and a thickness of approximately 0.8 mm) according to the relation:<sup>49,66</sup>

$$\varepsilon_{eq} = \frac{1}{\sqrt{3}} \frac{2\pi Nr}{t_D} \tag{2}$$

where r is the distance from the disk center, N is the number of HPT turns, and  $t_{\rm D}$  is the thickness of the disk. Since the strain proportionally increases with r, the microstructure and thus mechanical properties change within the 10-mmdiameter disk. Together with the limited sample size, such a local gradient makes the nanoindentation technique a strong tool for evaluating the mechanical properties of HTPprocessed materials.<sup>67)</sup> This is because nanoindentation testing has a simple and easy procedure and requires only a small volume of material. In addition, it has been reported that various mechanical properties beyond hardness and reduced modulus can be determined from the load (P) versus displacement (h) curves. Thus, there have been several studies reporting the use of nanoindentation testing for exploring the mechanical behavior of HPT-processed materials.<sup>40,67</sup> Accordingly, in this report the crucial results in nanoindentation studies to date are reviewed to provide insight into the effect of HPT-induced grain refinement on the deformation behavior of HEAs.

#### 2. Fundamental Applications of Nanoindentation: Hardness and Elastic Modulus

The primary objective of the nanoindentation test is to estimate the hardness,  $H_N$ , which is also useful for analyzing the effect of rate and temperature on the deformation behavior of a material as discussed below. The  $H_N$  is determined as

$$H_N = \frac{P_{max}}{A_c} \tag{3}$$

where  $P_{\text{max}}$  is the maximum load and  $A_c$  is the projected contact area that is a geometrical function of the contact depth,  $h_c$ . Based on the Oliver-Pharr method,<sup>68,69)</sup> the  $H_N$ value of a material can be extracted from the loaddisplacement (*P-h*) curve recorded during nanoindentation testing. For several HEAs, the nc structure can be obtained at the edge of the HPT disk even in the early stage of HPT processing.<sup>31,70)</sup> Therefore, the mechanical behavior of nc HEAs can be systematically explored by performing nanoindentation tests on the edge regions of HPT disks.

Figure 1 shows the variation in  $H_N$  of CoCrFeMnNi HEA as a function of the number of HPT turns, N. Nanoindentation hardness remarkably increases in the early stages of the HPT



Fig. 1 Variations in nanoindentation hardness ( $P_{\text{max}} = 100 \text{ mN}$ , Berkovich indenter) and microhardness ( $P_{\text{max}} = 980 \text{ mN}$ , Vickers indetner) of CoCrFeMnNi HEA as a function of  $N^{31}$  Note that all hardness values were taken at the edge of HPT disks.

process (N = 1/4 turn) and thereafter saturates toward the maximum values. Since HPT processing refined the grain size of CoCrFeMnNi HEA from an initial value of ~40 µm to ~40 nm without any phase transformation,<sup>31)</sup> HPT-induced hardening is mainly attributed to the grain refinement. It is also noteworthy that the tendency of the change in hardness is almost the same for the nanoindentation test and the microhardness test, but the higher values were recorded from nanoindentation tests compared with microhardness. This may be due to an indentation size effect (ISE) which is manifest as an increase in  $H_N$  with decreasing *h* for a sharp indentation.<sup>71,72</sup>

From nanoindentation tests, it is also possible to estimate the critical resolved shear stress required to operate plastic flow across the GB,  $\tau_c$ , based on the dislocation pile-up model as:<sup>73)</sup>

$$k_{HP} = 3M(\pi m_s \tau_c Gb/2\alpha)^{1/2} \tag{4}$$

where M is the Taylor factor (taken as 3.06 for FCC),  $m_s$  is Sachs orientation factor  $(2.2378^{74})$ , G is the shear modulus, b is the magnitude of the Burgers vector,  $\alpha$  is the average dislocation character obtained by  $\alpha = 2(1 - \nu)/(2 - \nu)$  ( $\nu$  is Poisson's ratio). Using eq. (4), the  $\tau_c$  value can be estimated from the  $H_{\rm N}$  versus  $d^{-1/2}$  plot whose slope indicates  $k_{\rm HP}$ . For example, it was reported for FCC structured CoCrFeNi MEA processed by HPT.<sup>52)</sup> Figure 2 shows the variation in  $H_N$  as a function of  $d^{-1/2}$  under different indentation strain rates,  $\dot{\varepsilon}_i = h^{-1} (dh/dt).^{52}$  For all  $\dot{\varepsilon}_i$ ,  $H_N$  versus  $d^{-1/2}$  plots are exactly following the Hall-Petch relation and the estimated values of  $k_{\rm HP}$  for the MEA are within the range of  $\sim 32.2$ - $33.4 \text{ MPa}(\text{mm})^{1/2}$ , which are similar to the values for CoCrFeMnNi HEA ( $\sim 27.7 \text{ MP}(\text{mm})^{1/231}$ ). Using eq. (4) and the  $k_{\rm HP}$  values obtained from Fig. 2, the  $\tau_{\rm c}$  values are calculated and summarized in Table 1. The values of  $\tau_c$  for the HEA were determined as  $\sim$ 138–149 MPa, which are much higher than those reported for pure FCC metals (e.g. 21.9 MPa for Cu and 36.7 MPa for Ni<sup>75</sup>), suggesting that the GB strengthening is more significant in FCC M/HEAs than in conventional FCC metals.



Fig. 2 Change in nanohardness ( $P_{\text{max}} = 100 \text{ mN}$ , Berkovich indenter) of CoCrFeNi HEA as a function of  $d^{-1/2}$  under different  $\dot{\varepsilon}_i$ .<sup>52)</sup> Note that all hardness values were taken at the edge of HPT disks.

The significant GB strengthening in FCC M/HEAs is often attributed to the severe lattice distortion, which results in high Peierls stress.<sup>76</sup> It is also noteworthy that the  $k_{\rm HP}$ values obtained from Fig. 2 are obviously higher than the  $k_{\rm HP}$  value (~21.8 MP(mm)<sup>1/2</sup>) reported for the CoCrFeMnNi HEA of which grain size was controlled through heat treatments. This discrepancy could be due to the fact that the Hall-Petch plot in Fig. 2 was analyzed without taking into account the effect of dislocation hardening. During HPT processing, a large number of dislocations can accumulate and hence further contribute to HPT-induced hardening as followed by Taylor equation ( $\sigma_{Taylor} = \alpha MGb \sqrt{\rho}$ , where  $\rho$ is dislocation density).<sup>77-80)</sup> Therefore, it should be noted that the  $k_{\rm HP}$  values presented in Fig. 2 and Table 1 might be overestimated due to the lack of consideration of dislocation hardening.

Recently, there have been several attempts to fabricate nanocomposites by performing the HPT processing on dualphase HEAs (such as  $Al_{0.7}CoCrFeNi$ )<sup>81)</sup> or two disks of HEAs with different phases.<sup>82)</sup> For example, Taheriniya *et al.*<sup>82)</sup> produced an FCC CoCrFeMnNi and BCC HfNbTaTiZr nanocomposite via HPT processing (Fig. 3(a)–3(e)) and reported that the microhardness of the composite was found to be superior to the HPT deformed single-phase matrices after the same number of revolutions, i.e., the imposed ideal shear strains (Fig. 3(f)). To gain an insight on the hardness distribution within the constituent phases, high resolution-high speed nanoindentation mapping was employed for the nanocomposite and the results are displayed in Fig. 4.<sup>82)</sup> As shown in Fig. 4(a), two distinct phases are clearly identified by the cluster maps and, more importantly, the average values of hardness for Phase 1 (i.e., FCC phase) and Phase 2 (i.e., BCC phase) gradually increase with increasing numbers of HPT turns. In addition, the hardness intensity maps in Fig. 4(b) clearly revealed that a significant increase in hardness was observed in Phase 2 near the interphase boundary, in which deformation-induced dislocation accumulation and element migration occurred.<sup>82)</sup>

Similarly, Gao et al.<sup>81)</sup> carried out nanoindentation on an HPT-processed dual-phase Al<sub>0.7</sub>CoCrFeNi HEA for exploring the contribution of constituent phases to its overall strength. Since the BCC/B2 phases (especially in HPTprocessed samples) are too small to be directly indented, the authors suggested the protocol to estimate the hardness of only BCC/B2 phase from the hardness of FCC + BCC/B2mixture, which is schematically illustrated in Fig. 5(a). As shown in the inset of Fig. 5(a), the indentation impressions produced at  $P_{\text{max}} = 10 \text{ mN}$  include both FCC and BCC/B2 phases. Therefore, the tests with  $P_{\text{max}} = 5 \text{ mN}$  were additionally performed on only the FCC phase. Since the  $H_{\rm N}$ obtained from FCC + BCC/B2 (i.e.,  $H_N$  at  $P_{max} = 10 \text{ mN}$ ) cannot be directly compared with the  $H_N$  obtained from the FCC phase (i.e.,  $H_{\rm N}$  at  $P_{\rm max} = 5 \,\text{mN}$ ) due to ISE,  $H_{\rm N}$  should be converted to the size-independent, mascroscopic hardness,  $H_0$  using the Nix-Gao model:<sup>71)</sup>

$$H_N^2 = H_0^2 \left( 1 + \frac{h^*}{h} \right)$$
 (5)

where  $h^*$  is a material length scale for *h*-dependent  $H_N$ . With the  $H_N$  versus *h* plot recorded during nanoindentation, eq. (5) enables us to estimate  $H_0$  of FCC + BCC/B2 and FCC phases, referred to as  $H_{0,all}$  and  $H_{0,F}$ , respectively (Fig. 5(a)). Then,  $H_0$  of the BCC/B2 phase,  $H_{0,B}$ , can be determined by using the simple rule-of-mixtures:

$$H_{0,B} = \frac{H_{0,all} - H_{0,F} X_F}{1 - X_F} \tag{6}$$

where  $X_{\rm F}$  is the fraction of FCC phase within the indentationinduced plastic zone volume. Since the radius of the plastic zone during indentation ( $r_{\rm p}$ ) is actually larger than the visible triangular impression,  $r_{\rm p}$  should be considered while calculating the  $X_{\rm F}$  value. According to Johnson's expandingcavity-based model,<sup>83)</sup>  $r_{\rm p}$  can be estimated as:

$$r_{p} = h_{c} \cot(90^{\circ} - \theta) \left\{ \frac{1}{6(1-\nu)} \left[ \frac{E}{\sigma_{y}} \tan(90^{\circ} - \theta) + 4(1-2\nu) \right] \right\}^{1/3}$$

$$(7)$$

where  $\theta$  is the half-cone angle to the surface (70.3° for Berkovich indenter) and  $\sigma_y$  is the yield strength (~701 MPa<sup>84</sup>). By drawing the circle with calculated  $r_p$ 

Table 1 The average values of  $H_0$ ,  $k_{\rm HP}$ , and  $\tau_c$  for the CoCrFeNi HEA.<sup>52)</sup>

$\dot{\varepsilon}_i$ [s <sup>-1</sup> ]	<i>H</i> 0 [GPa]	$k_{\rm HP} [{ m MPa}({ m mm})^{1/2}]$	τ <sub>c</sub> [MPa]
0.01	$2.034\pm0.130$	$32.2 \pm 1.2$	138
0.025	$2.083\pm0.129$	$33.0\pm1.0$	145
0.1	$2.158\pm0.152$	$33.4 \pm 1.2$	149



Fig. 3 SEM images and the corresponding EDS elemental maps of CoCrFeMnNi and HfNbTaTiZr nanocomposites processed by HPT after (a) N = 5, (b) N = 10, and (c) N = 15 along with (d) enlarged image of (c), (e) EDS line scan across different phases occurring in N = 10 sample, (f) results of microhardness test ( $P_{max} = 10$  N, Vickers indenter). Note that the individual concentration profiles are shifted in (e) for better visibility.<sup>82)</sup>

surrounding each indentation, the  $X_{\rm F}$  values can be calculated on the basis of a comparison of SEM images taken prior to and after nanoindentation. From the above process, the remaining value of  $H_{0,\rm B}$  can be finally obtained from eq. (7). Figure 5(b) shows the variations in  $H_0$  of each phase as a function of *N*. For clarifying the HPT-induced hardening, the hardening ratio, which is the hardness change divided by the original hardness, for each phase was summarized in Fig. 5(c). It can be seen that the hardening due to HPT is significant in both the FCC and BCC/B2 phases, but the hardening ratio of the FCC phase is always higher than that of the BCC/B2 phase. The above results imply that the nanoindentation technique can be utilized to decouple the distinct role of constituent phases in the mechanical behavior of nanocomposite HEAs. In addition to the hardness, nanoindentation testing can be used to determine the elastic modulus from the *P*-*h* curve through the relation:<sup>68,69</sup>

$$S = \beta \frac{2}{\sqrt{\pi}} E_r \sqrt{A_c} \tag{8}$$

where S is stiffness,  $\beta$  is a dimensionless parameter, and  $E_r$  is the reduced modulus defined by

$$\frac{1}{E_{eff}} = \frac{1 - v_s^2}{E_s} + \frac{1 - v_i^2}{E_i}.$$
(9)

The subscripts "s" and "i" denote the sample and indenter. Maier-Kiener *et al.*<sup>85)</sup> explored the evolution of hardness and elastic modulus of HPT-induced nc CoCrFeMnNi HEA upon post-process heat treatment. For 1 h isochronal annealing, the



Fig. 4 Results of nanoindentation on the HPT-induced CoCrFeMnNi and HfNbTaTiZr nanocomposites: (a) Cluster maps with two distinct phases and the average hardness of Phase 1 and 2 plotted for each sample; (b) Hardness intensity maps.<sup>82)</sup>

hardness of the nc HEA gradually increases with annealing temperature,  $T_A$ , and reaches a maximum value of  $\sim$ 7.64 GPa at  $T_A = 550^{\circ}$ C, beyond which it decreases to  $\sim 2.2$  GPa for  $T_{\rm A} > 800^{\circ}$ C (Fig. 6). Similarly, the modulus of nc HEA first increases to a maximum of 252 GPa at  $T_A = 550^{\circ}$ C, but remains fairly constant up to  $T_A = 700$  °C. Afterwards, the modulus decreases significantly for  $T_A > 800^{\circ}$ C. A detailed microstructural analysis by Schuh et al.<sup>36)</sup> reported that nanoscale precipitates (NiMn-, FeCo, and Cr-rich phases) formed in the primary single-phase matrix of nc CoCrFeMnNi HEA after annealing at 450°C for 1 h. The annealing at intermediate temperature (i.e.,  $550^{\circ}C < T_A < 800^{\circ}C$ ) led to coarsening of the FCC HEA matrix, but the secondary phases were still present at GBs and triple junctions.<sup>36)</sup> On this basis, a sudden increase in hardness and modulus at  $T_A = 450^{\circ}C$ could be attributed to the formation of secondary phases. For  $550^{\circ}C < T_A < 800^{\circ}C$ , hardness starts to decrease due to the grain growth, whereas the modulus is unaffected by grain size and therefore remains high. For  $T_A > 800^{\circ}$ C, the modulus drops significantly and converges to that for the nc HEA before annealing. This can be directly correlated to a complete dissolution of the nanophases and restoration of the single phase, as reported by previous microstructural analyses.36) Thus, the change in elastic modulus, rather than the change in hardness, can be directly related to the formation of additional phases during annealing. These results imply that nanoindentation of nc HEAs is a powerful tool to detect phase decomposition, which can also be used to qualitatively predict the long-term stability of single-phase HEAs.

#### 3. Stress-Strain Response for Plastic Flow

Since a sharper indenter induces a larger elasto-plastic strain in the material,<sup>86,87)</sup> a series of nanoindentation tests with numerous triangular pyramidal indenters having different "sharpness" that can be determined by centerline-to-face angle,  $\psi$ , makes it possible to estimate the constitutive stressstrain behavior of a local region within HPT-processed HEAs. This allows for systematic analysis of the effects of grain size on the stress-strain response and thus the constitutive behavior of HPT-processed HEAs. Such an example can be found in Lee et al.<sup>88)</sup> that explored the effect of annealing treatment on plastic flow in HPT-processed CoCrFeMnNi HEA. Figure 7 shows the variations in hardness (H) as a function of  $\psi$  (i.e., the sharpness of pyramidal indenter) for the HPT-processed CoCrFeMnNi HEA before (HPT) and after annealing treatment at 723 K for 1 h (HPT+1A) and 10 h (HPT+10A). For comparison purposes, the corresponding H versus  $\psi$  plot for the as-cast sample is also displayed in Fig. 7. As mentioned earlier, the indentations made with different  $\psi$  lead to different levels of plastic strain (so-called as characteristic strain,  $\varepsilon_{char}$ ) which can be described as<sup>89)</sup>



Fig. 5 (a) Schematic diagram of ISE calculation process for the HPTprocessed Al<sub>0.7</sub>CoCrFeNi HEA, the solid line is theoretical value of nanoindentation data, and the dashed line is the curve after ISE correction, (b) changes in  $H_0$  of uncharged and hydrogen-charged samples, and (c) hardening ratio by hydrogen charging and by HPT (inset) as a function of N.<sup>81)</sup>

$$\varepsilon_{char} = 0.2 \sqrt{\frac{\pi}{3\sqrt{3}}} \cot \psi \tag{10}$$

In addition, the *H* value obtained from each sharp indenter can be converted into corresponding flow stresses,  $\sigma_f$ , by using Tabor's well-known empirical relationship<sup>90</sup>

$$\sigma_f = \frac{H}{C_{\psi}} \tag{11}$$



Fig. 6 Nanoindentation results ( $h_{max} = 2500 \text{ nm}$ , Berkovich indenter) on CoCrFeMnNi HEAs with millimeter-sized grain (CH), micrometer-sized grain (MG), and HPT-processed nanocrystalline (NC) structure: (a) Hardness and (b) elastic modulus measured at room temperature after 1 h isochronal heat treatments at different annealing temperatures.<sup>85)</sup>

where  $C_{\psi}$  is the constraint factor. Although the value of  $C_{\psi}$  is typically in the range of 2.6–3.0 for metallic materials in the fully plastic regime of indentations, it strongly depends on  $\psi$  in the elasto-plastic regime:<sup>89)</sup>

$$C_{\psi} = \frac{2}{3} \left[ 2 + ln \left( \frac{1}{3} \frac{E}{\sigma_{y}} \sqrt{\frac{\pi}{3\sqrt{3}}} \cot \psi \right) \right]$$
(12)

where *E* and  $\sigma_y$  are elastic modulus and yield strength, respectively. Lee *et al.*<sup>88)</sup> estimated  $\sigma_y$  value for each condition using nanoindentation data obtained from  $\psi =$ 85°. Since sharp indenter with  $\psi = 85°$  can apply substantially low  $\varepsilon_{char}$  (~ 0.014), it is reasonable to assume that the corresponding  $\sigma_f$  is close to  $\sigma_y$ , details of which are provided in Ref. 88). Table 2 shows a summary of the  $C_{\psi}$  values calculated by eq. (12) for each condition. If the calculated  $C_{\psi}$  is higher than 3,  $C_{\psi} = 3$  was adopted instead of the calculated one, based on the assumption that a fullyplastic regime begins at  $C_{\psi} = 3$ .

With eq. (10)–(12) and Table 2, H vs.  $\psi$  data in Fig. 7(a) can be successfully converted into stress vs. strain plots as shown in Fig. 7(b), where the tensile stress-strain curve for the as-cast HEA is also shown. Except for a slight discrepancy in stress, which may be due to the ISE, the derived the trend of stress change with respect to strain (or strain-hardening behavior) of the as-cast HEA sample agrees well with tensile results.<sup>91</sup> It is interesting to find that the CoCrFeMnNi exhibits a transition from strain-hardening to



Fig. 7 (a) Variations in nanohardness ( $P_{max} = 100 \text{ mN}$ ) as a function of indetner angle and (b) the estimated stress-strain curves for as-cast CoCrFeMnNi HEA and HPT-processed nc CoCrFeMnNi HEA with or without isothermal annealing.<sup>88)</sup> The tensile test data for the as-cast HEA<sup>91</sup> is also shown for comparison purposes.

strain-softening as grain size reduces from  $\sim 40 \,\mu m$  (i.e., ascast sample) to  $\sim 40 \text{ nm}$  (HPT sample). Similar to conventional nc metals and alloys, an extensive dynamic recovery, dynamic recrystallization, and the existence of residual internal stress in GBs could be considered as the possible mechanisms for the strain-softening phenomena in nc CoCrFeMnNi HEA. Figure 7(b) also revealed that the quantity of strain-softening increases with the annealing time, indicating that an additional mechanism may be activated for the annealed HPT samples. Considering that the fractions of annealing-induced second phases (especially for the intermetallic NiMn and FeCo phases) were reduced with increasing  $\varepsilon_{char}$ , the deformation-assisted dissolution of the intermetallic phases could be the reason for the severe strain-softening behavior in the annealed HPT samples. The deformation-assisted destabilization of the second phases can be explained by taking into account the increase in the interface energy resulting from the dislocation accumulation and friction at the site.

#### 4. Rate-Dependent Plasticity: Estimation of Deformation Mechanism

The rate-dependent plasticity such as strain-rate sensitivity and activation volume permits a better understanding of thermally-activated plastic deformation mechanisms. Nanoindentation testing offers the advantage of being able to analyze the rate-dependent plasticity with reliability, since it can quickly generate a large amount of data and hence statistical analysis is feasible. Strain-rate sensitivity (*m*) and activation volume (*V*\*) can be estimated by nanoindentation tests in two different methods: multiple constant strain-rate (CSR) tests and single strain-rate jump (SRJ) tests. With the empirical relation between the uniaxial strain rate  $\dot{\varepsilon}$ and the indentation strain rate  $\dot{\varepsilon}_i$  (i.e.,  $\dot{\varepsilon} \approx \beta \dot{\varepsilon}_i$ , where  $\beta$  is constant<sup>92,93</sup>), *m* and *V*\* values can be expressed at a given strain,  $\varepsilon$ , and temperature, *T*, by

$$m = \left(\frac{\partial \ln \sigma_f}{\partial \ln \dot{\epsilon}}\right)_{\epsilon,T} = \left(\frac{\partial \ln(H/C_{\psi})}{\partial \ln(\beta \dot{\epsilon}_i)}\right)_{\epsilon,T}$$
(13)

and

$$V^* = \sqrt{3}kT \left(\frac{\partial \ln \dot{\varepsilon}}{\partial \sigma_f}\right)_{\varepsilon,T} \approx \sqrt{3}kT \left(\frac{\partial \ln(\beta \dot{\varepsilon}_i)}{\partial (H/C_{\psi})}\right)_{\varepsilon,T}, \quad (14)$$

where k is Boltzmann's constant. Note that  $C_{\psi}$  and  $\beta$  are often taken as ~3 and ~0.01, respectively, but they may vary with the material and loading condition.<sup>91,93)</sup> Therefore, m and V\* values can be determined from the slope of a  $\ln(H/C_{\psi})$  versus  $\ln(\dot{\varepsilon}_i)$  plot and the slope of the  $\ln(\dot{\varepsilon}_i)$  versus  $H/C_{\psi}$  plot, respectively. An example is shown in Fig. 8 that provides the variations in m and V\* of CoCrFeMnNi HEA as a function of HPT turns.<sup>31)</sup>

As shown in Fig. 8(a), the HPT process has a substantial effect on these rate-sensitive parameters, suggesting that the predominant deformation process in the HEA could be transformed by grain refinement. To better understand the effect of grain refinement on the deformation mechanism of HEAs, the *m* and  $V^*$  values of HEAs from the literature<sup>31,52,94–104</sup>) are plotted as a function of grain size, *d*, in Fig. 9. For comparison purposes, the literature data for pure Ni and binary Ni alloys<sup>105–113</sup>) are also present in Fig. 9. The *m* and  $V^*$  for those alloys are summarized in Table 3. Note that only the results for FCC HEAs are included in Fig. 9, since the variation in *m* value with *d* in BCC and HCP HEAs has not been extensively examined. For example, González-Masís *et al.*<sup>56</sup> investigated the rate-dependent plasticity in the HPT-processed Ti–Nb–Zr–Ta–Hf system

Table 2 Calculated  $C_{\psi}$  values in CoCrFeMnNi HEA.<sup>88)</sup>

	$\psi = 85^{\circ}$	$\psi = 75^{\circ}$	$\psi = 65.3^{\circ}$	$\psi = 50^{\circ}$	$\psi = 35.3^{\circ}$
As-cast	2.9	3.6	4.0	4.4	4.7
HPT	2.0	2.8	3.1	3.5	3.9
HPT+1A	1.8	2.5	2.9	3.3	3.6
HPT+10A	1.5	2.3	2.6	3.0	3.4



Fig. 8 Variations in (a) strain-rate sensitivity and (b) activation volume of HPT-processed CoCrFeMnNi HEA with increasing *N*. Stress versus strain rate and logarithmic strain rate versus linear stress plots are provided in the insets of (a) and (b), reespectively.<sup>31</sup> Note that nanohardness values were obtained under  $P_{\rm max}$  of 100 mN with Berkovich indenter.

through nanoindentation technique. However, the effect of element addition rather than the effect of grain size on strainrate sensitivity was mainly focused in their work; *m* value tends to decrease with increasing the number of elements  $(m \sim 0.011 \text{ for TiNb} \text{ and } m \sim 0.006 \text{ for TiNbZrTaHf}).^{56}$ 

For clarity, all the data in Fig. 9 are grouped into two separate ranges of d, i.e.,  $\sim$ 5–100 nm (nc range) and  $\sim$ 4–  $200 \,\mu\text{m}$  (cg range). In the nc regime, the *m* values for FCC HEAs ( $\sim 0.016-0.07$ ) are comparable to that for pure Ni ( $\sim$ 0.010–0.055), whereas in the cg regime, the *m* values show a significant discrepancy (~0.007-0.06 for HEAs vs.  $\sim$ 0.002–0.005 for Ni). These results indicate that the deformation mechanisms in nc HEAs and nc Ni are similar, whereas the deformation mechanism in cg HEA is considerably distinct from that in cg Ni. A similar conclusion can also be drawn from  $V^*$  versus d plots in Fig. 9(c) and 9(d). The  $V^*$  values for the conventional cg FCC metals and alloys are typically in the range of  $\sim 100-1000 \ b^3$ , corresponding to the dislocation forest cutting mechanism,<sup>114,115)</sup> as shown in Fig. 9(d). On the other hand, cg FCC HEAs exhibit significantly lower  $V^*$  values (usually in the range of  $\sim 10-100 \ b^3$ ), indicating that the short-range of barriers, which are responsible for thermal-activated deformation,<sup>105,114)</sup> are predominant. This might be due to the fact that HEAs have high lattice friction stress and hence the Peierls barrier to dislocation motion is much stronger than conventional FCC metals.<sup>97,116)</sup> In addition, the existence of chemical short-range ordering in the HEAs, which has been confirmed theoretically and/or experimentally,<sup>29-31)</sup> may also be responsible for its high friction stress and thus contribute to the low  $V^*$  values in the cg HEAs.<sup>97,102,116)</sup> By contrast, the  $V^*$  values for nc fcc HEAs and nc fcc metals are around  $\sim 10$  $b^3$ , suggesting that the deformation mechanism in the nc fcc HEAs is GB-mediated dislocation activity (e.g., dislocation nucleation and/or dislocation depinning at GBs<sup>105,106</sup>) as in the conventional nc FCC metals. Thus, it is concluded that the rate-limiting deformation mechanism in FCC HEAs transforms from lattice atoms-dislocation interaction to GBmediated plasticity as the d is reduced to nc regime.

# 5. Temperature-Dependent Plasticity: Estimation of Activation Energy

Since all mechanical properties such as H, m, and  $V^*$  are highly dependent on testing temperature, nanoindentation tests at various temperatures can provide crucial information for high-temperature (HT) applications of HEAs. Figure 10 shows the HT nanoindentation results obtained from CoCrFeMnNi HEAs with cg and HPT-processed nc structures.  $^{117)}$  As expected,  $H_{\rm N}$  of both nc and cg HEAs decreases with increasing T, but the slope of the  $\ln(H_N)$ versus 1/T plot is significantly changed at ~473 K only for nc HEA (Fig. 10(a)). A similar transition can also be captured in the variation in m as a function of T (Fig. 10(b)); the value of *m* remains nearly constant ( $\sim 0.015$ ) up to 423 K, then increases abruptly from 473 K onwards with T. Although sudden changes in  $H_N$  and *m* values at ~473 K indicate a possible transition in the deformation mechanism of nc HEA, it is challenging to confirm this mechanistic transition due to the lack of any substantial change in  $V^*$  across the whole examined T range (Fig. 10(c)). These tendencies are in a good agreement with the data reported by Maier-Kiener et al.,98) despite a slight discrepancy in absolute values. Therefore, an investigation of the apparent activation energy, Q, is essential for a complete understanding of the thermallyactivated deformation process. According to the Boltzmanntype constitutive law for temperature-dependent plastic strain rate,  $\dot{\varepsilon} = \dot{\varepsilon}_0 exp(-\frac{Q}{kT})$ , where  $\dot{\varepsilon}_0$  is a pre-exponential constant and the barrier Q is described as the stress-dependent Gibbs free energy  $\Delta \mathcal{G}$  for the activation of deformation. Considering that the entropy for deformation tends to be ignored due to its extremely small value,  $\Delta G$  is often assumed to be equal to the apparent activation enthalpy,  $\Delta \mathcal{H}$ .<sup>115,118)</sup> Then,  $\Delta \mathcal{H}$ can be expressed as:115,118)

$$\Delta \mathcal{H} = \frac{HV^*}{\sqrt{3}C_{\psi}} \frac{\partial(\ln H)}{\partial(1/T)} \tag{15}$$

Using eq. (15) and the *T*-dependent *H* data shown in Fig. 10(a), the  $\Delta \mathcal{H}$  for nc CoCrFeMnNi HEA at each testing temperature can be determined, and the change in  $\Delta \mathcal{H}$  with *T* is displayed in Fig. 10(d). For  $T \leq 473$  K (~ 0.3 $T_{\rm m}$ ), nc CoCrFeMnNi HEA shows a relatively low  $\Delta \mathcal{H}$  value (~0.5 eV). Since the activation barrier for the GB-mediated



Fig. 9 (a), (b) Strain-rate sensitivity and (c), (d) activation volume values of FCC metals and alloys. (a), (c) are for FCC HEAs,<sup>31,52,94–104)</sup> and (b), (d) are for pure Ni and binary Ni alloys.<sup>105–113)</sup>



Fig. 10 Results of the HT nanoindentation experiments on HPT-processed nc CoCrFeMnNi HEA: (a) the variation in nanohardness  $(h_{\text{max}} = 1700 \text{ nm}, \text{ Berkovich indenter})$  as a function of 1/T; (b) the changes in strain-rate sensitivity, (c) activation volume, and (d) apparent activation enthalpy as a function of  $T^{117}$ .

dislocation activities such as the emission of partial or perfect dislocations from GBs is expected as  $\sim$ 0.7–1 eV,<sup>105,119,120</sup>) the plastic deformation in nc CoCrFeMnNi HEA below a *T* of

473 K may be primarily governed by such a mechanism. For T > 473 K, however,  $\Delta \mathcal{H}$  of nc CoCrFeMnNi HEA abruptly increases to ~1.8 eV. This relatively high  $\Delta \mathcal{H}$  value is similar

Table 3 Summary of strain-rate sensitivity values and activation volume values for FCC HEAs,<sup>31,52,94–104)</sup> pure Ni,<sup>105–111)</sup> and binary Ni alloys.<sup>111–113)</sup>

Materials	Grain size, d [µm]	Strain-rate	Activation	Ref.
	100,110	sensitivity, m	volume, $V^*[b^3]$	07)
CoFeNi	100-110	0.055	62	97)
CoCrNi	100-110	0.040	4/	97)
CoCrFeNi	100-110	0.048	62	97)
	)/ 10.55	0.035	25	<u> </u>
	10-55	0.046	4.67	96)
	11	0.044	12	100)
	0.000	0.027	15	32)
	0.090	0.038	0	<u>90)</u> 52)
	0.076	0.027	0	52)
	0.040	0.024	0	52)
	0.045	0.017	8	101)
	0.020	0.040	0	101)
	1000	0.008	- 60	99)
	100-110	0.008	77	97)
	40	0.020	16	31)
	24	0.038	10	100)
CoCrFeMnNi	17	0.043	360	95)
	5	0.007	42	98)
	0.059	0.029	8	31)
	0.050	0.018	16	98)
	0.038	0.031	7	31)
	1000	0.017-0.020	263-284	102)
	150	0.064	-	104)
	100	0.012	54	103)
Al <sub>0.1</sub> CoCrFeN1	12	0.029	-	104)
	0.080	0.035	5	103)
	0.016	0.036	8.9	101)
	150	0.063	-	94)
Al <sub>0.3</sub> CoCrFeN1	0.013	0.023	13	101)
Ni-Co alloy	0.013	0.025	7	113)
	0.023	0.005		111)
NI: Es alles	0.022	0.010	23	112)
INI-re alloy	0.015	0.027	-	111)
	0.007	0.023	-	111)
	40		250	109)
Ni	40	0.005	1650	105)
	20	0.003	1900	110)
	10	0.003		107)
	0.040	0.030		108)
	0.030		10	109)
	0.029	0.019	11	105)
	0.021	0.020	118	110)
	0.021	0.053		110)
	0.020	0.055	11	106)
	0.020	0.010	14	100)
	0.020	0.020	I	107)

to that of GB diffusion of Ni in CoCrFeMnNi HEA (i.e.,  $\sim 2.3 \text{ eV}^{121}$ ), suggesting that GB diffusion becomes pronounced for T > 473 K. This can be rationalized by

considering the large volume fraction of non-equilibrium GBs in HPT-processed nc HEA.<sup>36)</sup> Thus, the sharp change in the deformation behavior of nc HEA observed for T above



Fig. 11 Results of nanoindentation creep tests with Berkovich indenter on HPT-processed Al<sub>0.1</sub>CoCrFeNi HEA: (a) Creep displacement versus time; (b) double logarithmic plot between nanoindentation hardness and time.<sup>103)</sup>

473 K can be attributed to the enhanced plasticity due to GB diffusion.

#### 6. Room-Temperature Nanoindentation Creep Behavior

Due to the large fraction of non-equilibrium GBs in the HPT-processed HEAs, the diffusion-related process such as creep deformation could be enhanced in the alloys even at relatively low temperatures such as RT.<sup>70,103</sup> Therefore, the research of creep behavior at RT is crucial for evaluating the mechanical robustness of HPT-processed HEAs in a continuous mechanical load environment. Among various nanoindentation creep testing methods, the most popular by far is the constant-load method; the sample is quasi-statically loaded to a predetermined peak load, then the load is held constant, and the increase in h with holding time,  $t_{hold}$ , is recorded. This popularity is simply due to its close resemblance of the procedure to that in the conventional uniaxial creep test. From the change in h with t data, the variation in  $\sigma_{\rm f}$  (converted from *H* using eq. (11)) as a function of t can be obtained. To determine  $\dot{\varepsilon}_i = (dh/dt)/h$  for the creep regime, the displacement rate (dh/dt) is often calculated by fitting the *h* versus  $t_{hold}$  plot with an empirical equation:122,123)

$$h(t_{hold}) = h_0 + At_{hold}^{\kappa} + Bt_{hold} \tag{16}$$

where  $h_0$  is the indentation depth at load-hold at peak load, and A, B, and  $\kappa$  are fitting constants. The steady-state creep strain rate,  $\dot{\varepsilon}_{i,ss}$  and the applied stress,  $\sigma_{\rm f}$ , are usually correlated via an empirical power-law creep equation  $\dot{\varepsilon}_{i,ss} \propto \sigma_f^n$ , where n is the creep stress exponent. Therefore, the nvalue can be determined by log-log plotting of  $\sigma_{\rm f}$  against  $\dot{\varepsilon}_{i,ss}$ .

Although a sharp indenter like a three-sided pyramidal Berkovich indenter is widely used for nanoindentation creep test, some critical differences in data between indentation creep and uniaxial creep have been reported not only for conventional metals and alloys,<sup>123,124</sup>) but also for HEAs.<sup>70,103</sup> For example, Yu *et al.*<sup>103</sup> examined the creep resistance of HPT-processed Al<sub>0.1</sub>CoCrFeNi HEA by nano-

indentation equipped with a Berkovich indenter. Figure 11(a) shows the h versus  $t_{hold}$  plots obtained at the points of different distances from the disk center (r = 0 mm, 3 mm, and5 mm). The h versus  $t_{hold}$  curves are somewhat analogous to the early stages of the typical high-temperature creep curves, including both transient and steady-state creep regimes. The amount of creep displacement increases from 4.12 nm to 12.08 nm from the center (r = 0 mm) to the edge (r = 5 mm), implying that the creep deformation of the HEA is indeed enhanced by grain refinement. As shown in Fig. 11(b), however, the estimated n values  $(n \sim 83)$  for  $r = 0 \text{ mm}, n \sim 41 \text{ for } r = 3 \text{ mm}, n \sim 29 \text{ for } r = 5 \text{ mm}$ ) are unreasonably high, so that it is difficult to identify the underlying mechanism of creep deformation. This implausible creep behavior might arise from some critical issues related to the sharp tip geometry. Detailed explanations for these issues are introduced elsewhere.<sup>124)</sup>

To solve the issues related to sharp tip geometry, Lee *et al.*<sup>70)</sup> employed a spherical indenter to explore the creep behavior of the HPT-processed CoCrFeMnNi HEA. In spherical indentation,  $\varepsilon_{char}$  in eq. (10) can be quantified as  $0.2\sqrt{2hR - h^2}/R$  where *R* is the radius of the spherical indenter. As demonstrated in the inset of Fig. 12(a) and 12(b), creep deformation occurs even at RT in both cg and nc HEAs and, more importantly, the amount of creep strain ( $\varepsilon_{creep} = \varepsilon - \varepsilon_0$ , where  $\varepsilon_0$  is the strain at the onset of creep) clearly increases as  $P_{max}$  increases. To estimate the  $\dot{\varepsilon}_i$  for the spherical indentation,  $\varepsilon_{creep}$  versus  $t_{hold}$  curves were fitted according to Garofalo's mathematical fitting equation,<sup>125)</sup>

$$\varepsilon_{creep} = I(1 - e^{-\Phi t_{hold}}) + \chi t_{hold} \tag{17}$$

where I,  $\Phi$ , and  $\chi$  are fitting constants. By differentiating the fitted equation with respect to  $t_{hold}$ , the variations in  $\dot{\varepsilon}_i$  can be obtained as a function of  $t_{hold}$ . As shown in the main plots of Fig. 12(a) and 12(b),  $\dot{\varepsilon}_i$  versus  $t_{hold}$  curves of both cg and nc HEAs suggests the possibility of a close approach to the steady-state condition (or quasi-steady-state, QSS). Based on the variations in  $\dot{\varepsilon}_{i,ss}$  with  $\sigma_f$  (or  $P/\pi C(2hR - h^2)$  in spherical indentation) seen in Fig. 13, n was calculated to be 1 for nc HEAs and 3 for cg HEAs, implying that the governing



Fig. 12 Results of nanoindentation creep tests with spherical indenter on CoCrFeMnNi HEAs: Strain rate versus holding time (with the inset showing creep strain versus holding time) for (a) HPT-processed nc HEA and (b) as-cast cg HEA.<sup>70</sup>

mechanism of creep deformation transforms from dislocation-mediated mechanisms to diffusion-related processes as *d* reduces to within the nanoscale regime. Since the influence of GB diffusion on  $\dot{\varepsilon}_{i,ss}$  of nc HEAs is substantially larger than that of lattice diffusion, GB diffusion and its related deformation mechanisms, such as Coble creep, GB sliding, GB migration, and GB rotation, mainly dominate the creep deformation of nc HEA. In addition, the estimation of creep rate in FCC-structured nc HEA and its comparison with that in conventional nc metal with an fcc structure (i.e., Ni)



Fig. 13 Relations between quasi-steady state (QSS) creep strain rate and stress for HPT-processed nc CoCrFeMnNi HEA.<sup>70)</sup>

demonstrated that the creep resistance of nc HEA is significantly enhanced by sluggish diffusion in the HEAs.

### 7. Investigation of Hydrogen Effect on Mechanical Behavior

For practical applications of nc HEAs developed with the aid of HPT, it is crucial to demonstrate that their prominent mechanical performance is preserved even under a harsh environment such as a hydrogen atmosphere. Since the susceptibility of materials to hydrogen embrittlement (HE) is strongly correlated with their microstructure, the large fraction of GBs in nc HEAs may lead to significantly different HE behavior compared to cg HEAs. To shed light on this, Zhao et al.<sup>126)</sup> investigated the hydrogen absorption and its effect on the hardness of two nc HEAs (i.e., CoCrFeNi and CoCrFeMnNi) and compared the results with those obtained from cg counterparts. As shown in Fig. 14(a), a clear increase in  $H_N$  upon hydrogen charging is observed in all cases. Importantly, the percentage increase in  $H_{\rm N}$  is much smaller in both nc HEAs ( $\sim$ 7%) whereas it is substantial in cg samples (~57% for CoCrFeMnNi and ~29% for CoCrFeNi). On the basis of these results, it is reasonable to speculate that the effect of hydrogen on ductility/toughness



Fig. 14 (a) Changes in hardness due to hydrogen charging in CoCrFeNi and CoCrFeMnNi HEAs. (b) Activation volume (V\*) in both uncharged and hydrogen-charged HEAs.<sup>126)</sup>

may be weaker in nc HEA than in cg HEA. Insights into the possible reasons can be gained by analyzing the deformation mechanisms inferred through the  $V^*$  values. For the uncharged samples,  $V^*$  values in the nc HEAs are in the range of  $\sim 11-18 b^3$ , whereas  $V^*$  of the cg samples varies between  $\sim$ 22 and 70  $b^3$  (Fig. 14(b)), which is consistent with the literature data in Fig. 9(c) and Table 3. On the other hand, V\* values obtained on hydrogen-charged samples are always lower than those of the uncharged ones, implying that the absorbed hydrogen increases the lattice friction stress for dislocation motion. Such an enhancement in the friction stress inhibits dislocation mobility, leading to an increase in hardness with a reduction in  $V^*$ , which might eventually enhance the alloy susceptibility to HE. Such a contribution, however, would be negligible in nc HEAs, since the deformation in nc HEAs is mainly dominated by GBmediated plasticity rather than by lattice atoms-dislocation interaction, as deduced from the above analysis on  $V^*$ . As noted from Fig. 5(b) and 5(c), a similar trend also could be observed in dual-phase Al<sub>0.7</sub>CoCrFeNi HEA; hydrogeninduced hardening is significantly reduced after HPT processing for both FCC and BCC/B2 phases. Interestingly, the FCC phase shows much stronger hydrogen-induced hardening than the BCC/B2 phase. This is because the FCC phase absorbs much more interstitial hydrogen than BCC/ B2.<sup>127)</sup> In addition, the FCC phase is relatively softer than the BCC/B2 phase, making it more amenable to hydrogeninduced solid solution strengthening.87,128)

#### 8. Conclusions

Due to the extremely high straining, HPT processing can achieve exceptional grain refinement from cg to nc in various HEAs. To gain insights into the relationship between refined microstructure and mechanical behavior of HPT-processed HEAs, the nanoindentation technique has been widely employed under a variety of strain-rate and temperature conditions, allowing for exploring various mechanical properties of the local regions within an HPT disk. This review mainly focused on the results of nanoindentation research on HPT-processed HEAs with the following aspects:

- (1) The calculated  $H_N$  values of HEAs increase with increasing HPT turns, which is mainly due to GB strengthening. Especially for the HPT-fabricated nano-composite HEAs, the distinct role of constituent phases in their mechanical behavior could be additionally investigated through nanoindentation testing. Nevertheless, analyzing the change in elastic modulus is more successful than examining the change in hardness for detecting the phase transformation during post-process annealing.
- (2) It is feasible to estimate the constitutive stress-strain behavior for the large plastic regime of HPT-processed HEAs by performing a series of nanoindentation tests with a variety of sharp tips having different sharpness. It was revealed that annealing treatment on the HPTprocessed CoCrFeMnNi HEA resulted in a significant strain-softening behavior, which may be attributed to the deformation-induced dissolution of the intermetallic phase.

- (3) To investigate the rate-dependent plastic deformation which is related with enhancement in ductility of ufg and nc materials processed by HPT, the *m* and V\* values can be estimated by using nanoindentation tests. The *m* and V\* values obtained suggested that GBmediated dislocation activities are the predominant deformation mechanism in HEAs as in the conventional nc metals and alloys.
- (4) Through high-temperature nanoindentation tests, it is possible not only to measure temperature-dependent  $H_{\rm N}$  data but also to completely understand a thermally-activated plastic deformation process through estimating the activation energy. In the nc CoCrFeMnNi HEA, the contribution of GB diffusion to plasticity became pronounced for T > 473 K ( $\sim 0.3T_{\rm m}$ ).
- (5) Due to the large fraction of non-equilibrium GBs in nc HEAs processed by HPT, creep deformation can occur even at RT. For exploring creep mechanisms, the spherical indentation creep test is more reliable than the sharp indentation creep test. Although the creep deformation of CoCrFeMnNi HEA could be promoted by HPT processing, the resistance to creep in the nc HEA is superior to that of conventional nc Ni.
- (6) To examine nc HEA behavior in harsh service environments, the hydrogen effects on their mechanical behavior have been investigated through nanoindentation experiments.

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