Spherical nanoindentation creep behavior of nanocrystalline and coarse-grained CoCrFeMnNi high-entropy alloys

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Abstract

Time-dependent plastic deformation behavior of nanocrystalline (nc) and coarse-grained (cg) CoCrFeMnNi high-entropy alloys (HEAs) was systematically explored through a series of spherical nanoindentation creep experiments. High-pressure torsion (HPT) processing was performed for achieving nc microstructure in the HEA, leading to a reduction in grain size from ~46 μm for the as-cast state to ~33 nm at the edge of the HPT disk after 2 turns. Indentation creep tests revealed that creep deformation indeed occurs in both cg and nc HEAs even at room temperature and it is more pronounced with an increase in strain. The creep stress exponent, n, was estimated as ~3 for cg HEA and ~1 for nc HEA and the predominant creep mechanisms were investigated in terms of the values of n and the activation volumes. Through theoretical calculations and comparison of the creep strain rates for nc HEA and a conventional face-centered-cubic nc metal (Ni), the influence of sluggish diffusion on the creep resistance of nc HEA was analyzed. In addition, sharp indentation creep tests were performed for comparison purposes and the results confirmed that the use of a spherical indenter is clearly more appropriate for investigating the creep behavior of this HEA.

1. Introduction

High-entropy alloys (HEAs) containing five or more elements in almost equal atomic proportions, exhibit high strengths, large strain hardening capability, high toughness, excellent resistance to high-temperature softening and creep, and good tribological properties. Hence, these are emerging as an exciting class of new structural materials and are drawing considerable attention in terms of research [1–8]. Despite a large number of principal elements, HEAs can often form simple solid solutions due to high configurational entropy [1–4]. It is well known that the mechanical performance of a material can be substantially enhanced by imparting a finer microstructure to it. In fact, nanocrystalline (nc) metals and alloys (having average grain size, d < 100 nm) exhibit improved mechanical properties in comparison with their coarse-grained (cg) counterparts [9–13]. Then, it may be possible to achieve significantly improved materials by incorporating both the advantages of HEA and nc structure and, in fact, the authors’ previous study [14] reported that nc CoCrFeMnNi HEA exhibits significant strengthening and reasonably high plasticity both of which were achieved by extensive grain refinement.

Hitherto, nc HEAs have been synthesized by magnetron sputtering (MS) [15], mechanical alloying (MA) [16–19], and high-pressure torsion (HPT) [14,20,21]. Among them, HPT may be the most effective single-step processing to directly achieve...
excellent grain refinement in fully-dense bulk solids [22] because the sample synthesized by MS is only in thin film form and MA processing inevitably requires additional steps of consolidation. In addition, ability to achieve grain refinement in HEAs may be much higher in HPT than in MA, which can be supported by the fact that the average d of HPT processed CoCrFeMnNi alloys (~38–59 nm [14,21]) is reported to be significantly smaller than that of the same component nc HEA processed through MA followed by spark plasma sintering (~50–200 nm [19]).

In the case of exceptionally fine-grained materials processed by severe plastic deformation (SPD) including HPT and equal-channel angular pressing (ECAP), the large fraction of grain boundaries (GBs) are often considered to be in a non-equilibrium state [21,23–30]. These severe-strain-induced non-equilibrium GBs contain an excess of extrinsic dislocations, higher energy, and larger free volume or vacancy concentration than in normal GBs in cg or annealed materials [27]. This, in turn, can result in significantly faster diffusion along non-equilibrium GBs than along normal GBs [25–27]. Due to this specific feature of a large portion of non-equilibrium GBs, materials processed by ECAP or HPT often exhibit diffusion-related deformation processes such as GB sliding and creep even at relatively low temperatures [10,31,32]. By comparison with ECAP, HPT processing has the advantage of introducing higher plastic strains and hence producing finer structures and a higher fraction of high-angle GBs [33–35], thereby facilitating the occurrence of diffusion-related phenomena.

HEAs are well known to exhibit improved diffusion resistance due to the different local cohesive energy at any lattice site as well as the lattice distortion arising from the difference in atomic size of the constituent elements [36,37]. Thus, the creep behavior of nc HEAs may conceivably be different from conventional nc metals and alloys as well. However, only a few studies have been performed thus far to examine the creep behavior of nc HEAs. Chang et al. [38] performed creep tests on nc (AlCrTaTiZrN) coatings and investigated the influence of N addition on creep strain rate quantitatively. Ma et al. [15] studied the effects of peak load and loading rate on the creep deformation in a nc CoCrFeNiCu HEA thin film. However, almost no effort has been made to systematically indentify the creep mechanism of nc HEAs or to investigate the influence of sluggish diffusion on the creep properties of nc HEAs.

Based on this background, we explored time-dependent plastic deformation of nc HEAs in the present research through a series of spherical nanoindentation creep experiments. In general, the microstructure of HPT-processed material varies locally across the disk, therefore mechanical properties of HPT-processed metals have been extensively investigated through nanoindentation tests which require only a very small volume of material [14,39,40]. In this regard, nanoindentation creep testing [41–44] (especially, with a spherical tip; as we discuss later) is a promising way to successfully investigate small-scale creep behavior of HPT processed disks. Here, a CoCrFeMnNi HEA, which is one of the most widely studied HEA, was processed by HPT, and it was confirmed that the nc structure is readily achieved in the early stage of HPT processing. Thereafter, spherical nanoindentation creep experiments were performed on the nc HEA as well as their cg counterpart (i.e., as-cast HEA) for comparison purposes. The results revealed that the creep mechanism of nc HEA is different from that of cg HEA. By comparing the theoretically calculated creep strain rates of nc HEA to that of conventional face-centered-cubic (fcc) nc Ni, it is feasible to discuss the influence of sluggish diffusion on creep resistance of nc HEA.

2. Experimental

The alloy examined in this work was prepared by arc-melting a mixture of pure metals (purity >99 wt.%) having a nominal composition of Co20Cr20Fe20Mn20Ni20 (in atomic %) in a Ti-gettered high-purity Ar atmosphere. The ingots were remelted at least four times to promote chemical homogeneity. The melted alloys were then drop-cast into a mold with dimensions of 10 mm × 10 mm × 60 mm.

The as-cast samples (disks having a radius of 5 mm and a thickness of 0.83 mm) were subjected to HPT at room temperature (RT) with a pressure of 6.0 GPa for a total of either 1/4 or 2 turns using a rotational speed of 1 rpm [14]. To investigate the influence of straining on the quasi-static mechanical properties during HPT, the Vickers indentation hardness, HV, was measured using an HMV-2 microindenter (Shimadzu, Tokyo, Japan) at a peak load Pmax of 980 mN along diameters of the HEA disks processed by HPT. For each measurement position, the average value of HV was determined from four separate measurements recorded at uniformly separated points displaced from the selected position by a distance of 0.15 mm [45]. The microstructures of the specimens were examined using an optical microscope (CK40M, Olympus, Tokyo, Japan), an electron backscattered diffraction (EBSD) instrument (FEI XL30 FEG, Philips, Cambridge, UK), and a transmission electron microscope (Tecnai F20, FEI Co., Hillsboro, OR). For the optical microscopy observations, the samples were mechanically polished to a mirror-like finish and etched with aqua regia solution which is a mixture of nitric acid and hydrochloric acid in a volume ratio of 1:3. The sample for the EBSD measurements was prepared by mechanical polishing with 0.05 μm colloidal silica and subsequent electrolytic polishing at 58 V for 20 s in a mixture of 90% acetic and 10% perchloric acid at RT. Samples for transmission electron microscopy (TEM) at the vertical cross-sections of the HPT-processed disks were obtained through focused ion beam (FIB: Nova 200 NanoLab, FEI Co., Hillsboro, OR) milling. A thin layer was milled by FIB in the through-thickness direction at the edges of the processed HEA disks and lifted for TEM.

For the nanoindentation tests, electrolytic polishing at 58 V for 50 s in a mixture of 90% acetic and 10% perchloric acid was performed on mirror-finished samples to remove any possible surface damage induced during prior mechanical polishing. Nanoindentation creep experiments were performed at the edge regions, within 0.3 mm from the edge, of the HPT disks using a Nanoindenter-XP (formerly MTS; now Keysight, Santa Rosa, CA) with two different indenters, i.e. a Berkovich tip and a spherical tip with R = 38.6 μm (which was estimated by Hertzian contact analysis [46] of the indentations made on fused quartz). During testing, the specimen was loaded to different Pmax at a constant loading rate (dP/dt) of 0.5 mN s−1, held at Pmax for 1000 s, and fully unloaded. More than 10 tests were conducted for each testing condition.

For analyzing the applied strain variation within the HPT disk, finite-element analysis (FEA) simulation was performed using ABAQUS (HKS Inc., Pawtucket, RI) software. The geometries of the anvils were designed based on the quasi-constrained HPT conditions [47] and meshes were generated with 46,620 elements in the disk having initial l and r of 0.8 mm and 5.0 mm, respectively. A high friction coefficient of 0.7 was applied between the anvils and the disk to maintain a reasonable traction between them [47]. The material parameters used for the present simulation were based on the flow curve reported for this specific HEA [48].

3. Results

3.1. Achievement of nanostructures by HPT process

During the HPT, the equivalent von Mises strain εeq imposed on the disk is given by the relationship [49]

\[
ε_{eq} = \frac{3}{2} \frac{P_{max} R}{H} \left(1 - \frac{R}{2h}ight) \left(1 - \frac{r}{R}ight) \left(1 - \frac{R}{2r}ight)
\]
where $r$ and $t$ are the radius and thickness of the disk, respectively, and $N$ is the number of torsional revolutions. In Fig. 1, the changes in $H_V$ are represented as a function of $e_{eq}$ calculated from Eq. (1), and $H_V$ of the as-cast sample $(1.75 \pm 0.04 \text{ GPa})$ is also displayed. Note that $H_V$ in the figure is the Meyer's hardness which is equivalent to $P_{max}$ divided by projected area instead of the surface area (that is typically used for Vickers hardness). The inset of Fig. 1 provides the FEA simulation results for the $e_{eq}$ distribution over the one-quarter disk after ~1/4 turn that are illustrated through a series of colors representing the different listed strains. As shown in the figure, the values of simulated $e_{eq}$ at the edge of disk match well with those calculated according to Eq. (1).

From Fig. 1, three points are noteworthy. First, in the region of $e_{eq} \sim 5$–7, $H_V$ values for $N = 1/4$ overlap reasonably well with those for $N = 2$, implying that the two cases examined here ($N = 1/4$ and 2) can cover a wide range of straining in the HPT process. Second, at the early stage of HPT ($e_{eq} < 5$) the hardness of the processed disks increases rapidly with $e_{eq}$. After 1/4 turn, the $H_V$ at the disk edges (where $e_{eq} \sim 5$) reaches $4.70 \pm 0.04 \text{ GPa}$ which is almost three times higher than for the as-cast specimen $(1.75 \pm 0.04 \text{ GPa})$. Third, with further increasing of $e_{eq}$, the $H_V$ values throughout the disks increase moderately and then become saturated at around 5.2 GPa. These results demonstrate that this alloy experiences a significant strain hardening in the early stage of HPT processing and the strengthening exhibits saturation behavior around $e_{eq}$ of ~20.

The inhomogeneous distribution of $H_V$ in Fig. 1 supports the expectation that microstructural evolution will occur most significantly in the peripheral regions of the HPT processed disks. Fig. 2 shows representative microstructures of the as-cast sample and the edges of the HPT disks for $N = 1/4$ and 2 turns. Fig. 2a is an optical micrograph showing the dendritic microstructure in the as-cast sample. It was reported that the dendritic areas are slightly enriched with Cr, Co, and Fe, whereas the interdendritic areas have slightly higher Ni and Mn [50]. To acquire information on the true grain size instead of the dendrite size, EBSD analysis was conducted on the as-cast sample and a representative image combining index of quality and grain orientation map is shown in Fig. 2b where the average grain size, $d$, was determined as ~46 µm. After HPT processing, it was necessary to use TEM analysis to measure the grain sizes at the edge regions of the HPT disks. Fig. 2c and d shows bright-field (BF) images and selected area diffraction (SAD) patterns of the disk edges for $N = 1/4$ and 2, respectively. These micrographs show there are equiaxed fine grains with $d$ of ~49 and ~33 nm for 1/4 and 2 turns, respectively, which are similar to the data previously reported under the same conditions [14]. The SAD patterns for both samples confirm a single-phase fcc structure, indicating the absence of any phase transformation during the HPT processing, which is consistent with the x-ray diffraction data in the authors’ previous study [14]. From these results, it is concluded that nc structure develops in the early stages of HPT processing itself, and thereafter a gradual reduction in $d$ occurs with further turning. Considering the plateau in hardness (see Fig. 1), it is reasonable to believe that the grain refinement reaches a saturation level at the disk edge for $N = 2$.

3.2. Spherical indentation creep test

To compare the creep responses of nc and cg HEAs, modified constant-load nanoindentation creep experiments with a spherical indenter [13,44] were performed at the edges of the HPT processed disks as well as the as-cast sample. For classifying the data from different $P_{max}$, under elastic and elastic–plastic regimes, we conducted normal quasi-static nanoindentation tests without peak-load holding. Fig. 3 shows representative quasi-static nanoindentation load–displacement ($P–h$) curves of cg (as-cast) and nc HEAs. The $P–h$ curves obtained at relatively low $P_{max}$ (see blue open circle data in the curves) show that the loading part of each curve is completely reversed upon unloading, indicating that the deformation is purely elastic and follows the Hertzian contact theory [46]. In the case of cg HEA, sudden displacement excursions (often referred to as “pop-ins”) were observed at $P < 5$ mN during the loading sequence, and the displacements were not fully recovered on unloading. This suggests that yielding of the cg HEA under quasi-static loading occurs at a $P$ of around 5 mN. By contrast, the nc HEAs exhibit smooth elastic-to-plastic transition behavior (that may be due to the accumulation of small pop-ins) which correspond to the point where the experimental $P–h$ data deviate from the Hertzian curves. From Fig. 3, we can determine that the transition of nc HEAs occurs at $P$ around 8 and 10 mN for $d$ of ~49 and 33 nm, respectively. Fig. 4a and b shows the representative $P–h$ curves recorded during the spherical indentation creep tests performed in the elastic and elastic–plastic regimes, respectively. In both regimes, $h$ increases during the holding sequence so that creep occurs. Especially in the elastic regime, an increase in $h$ during the holding sequence can be clearly seen and this time-dependent deformation is mostly not recovered and remains upon unloading, thereby suggesting that the observed creep behavior is primarily plastic in nature and the possible contribution of anelasticity to the creep deformation is probably negligible. From the Hertzian contact analysis [46] of the loading curve in Fig. 4a, the plane-strain moduli of the samples, $E_0/[(1–ν^2)]$, where $E_0$ and $ν$ are Young’s modulus and Poisson’s ratio of the sample, respectively, were estimated as $193 \pm 5$ and $173 \pm 4$ GPa for cg and nc HEAs, respectively. Note that the value of cg HEA is in reasonable agreement with the literature data (~182 GPa) [51]. This confirms that creep plasticity can be generated at RT even if the stress state underneath the indenter is less than the global yield strength.

The total creep displacements, $h_{\text{creep}}$ (that is the maximum value of $h–h_0$ at 1000 s, hereinafter subscript 0 indicates the onset of creep) versus indentation strain at the onset of creep, $(e_{i0})$, for nc and cg HEAs are summarized in Fig. 5. In the case of spherical indentation, indentation strain, $e_i$, is often described as $0.2a/R_0$.
where $a$ is the contact radius and $R_i$ is the radius of the spherical indenter [46]. In the plot, the average values of stain estimated from elastic-to-plastic transition, $\varepsilon_y$, for nc and cg HEAs are represented with vertical lines. While the creep behavior is less pronounced in the elastic regime, the $\varepsilon_{\text{creep}}$ values in the elastic-plastic regime are relatively large and increase dramatically with $\varepsilon_i$.

As a first step to quantitatively analyze the creep behavior, the indentation creep strain, $\varepsilon_{\text{creep}}$, is quantified as $0.2(a-a_0)/R$ where $a$ is estimated as $a = \sqrt{2hR - h^2}$ in simple consideration of the contact geometry of a spherical indentation [43]. Note that in this study, a measured $h$ is used for simplicity instead of the precise value of contact depth, $h_c$. The examples of calculated results for nc and cg HEAs are described in the insets of Fig. 6 as a function of holding time ($t_{\text{hold}}$). The $\varepsilon_{\text{creep}}$ vs. $t_{\text{hold}}$ curves are somewhat analogous to the early stages of the typical high-temperature creep curves, consisting of both transient and steady-state creep regimes. It is also noteworthy that the amount of $\varepsilon_{\text{creep}}$ increases significantly with $P_{\text{max}}$, which indicates that the observed creep behavior is not an artifact caused by thermal drift that is independent of load [43,52,53].

To estimate the indentation strain rate, $\dot{\varepsilon}_i$, for a spherical indentation, $\varepsilon_{\text{creep}}$ vs. $t_{\text{hold}}$ curves were fitted according to Garofalo’s mathematical fitting equation which was originally developed for uniaxial creep tests,

$$\varepsilon_i - (\varepsilon_i)_0 = \varepsilon_{\text{creep}} = \dot{\varepsilon}_i = \varepsilon_{\text{creep}} = \alpha \left( \frac{1 - e^{-t_{\text{hold}}}}{1 - e^{-t_{\text{hold}}}} \right) + \omega t_{\text{hold}}$$

(2)

where $\alpha$, $\omega$ and $r$ are creep constants. By differentiating the fitted equation with respect to $t_{\text{hold}}$, the change in $\dot{\varepsilon}_i$ can be obtained as a function of $t_{\text{hold}}$. Applying the empirical relation between uniaxial strain rate, $\dot{\varepsilon}_u$, and $\dot{\varepsilon}_i$ of $\dot{\varepsilon}_u \sim 0.01\dot{\varepsilon}_i$ [54], the variations in $\dot{\varepsilon}_u$ with $t_{\text{hold}}$ for nc and cg HEAs are plotted in the main plots of Fig. 6. These results suggest the possible attainment of steady-state (hereinafter called “quasi-steady-state, QSS”) during indentation.

4. Discussion

4.1. Stress exponent, activation volume, and creep mechanism

Estimating the predominant creep mechanism is essential for...
better understanding of the creep behavior of HEAs. It is well accepted that the creep stress exponent, \( n = \frac{\partial \ln \varepsilon_{SS}}{\partial \ln \sigma} \) where \( \varepsilon_{SS} \) is the steady-state creep rate and \( \sigma \) is the applied stress), is a useful indicator for deducing the mechanism such that \( n = 1 \) for diffusion creep such as Nabarro–Herring creep (by lattice diffusion) and Coble creep (by GB diffusion), \( n = 2 \) for GB sliding, and \( n = 3 \)–8 for dislocation creep [55,56]. For comparison purposes, one can find summary tables of the \( n \) and other creep properties of a conventional nc fcc metal (Ni) estimated from various experiments [43,57].

In this study, from spherical indentation creep data the values of \( n \) can be directly obtained by using the equation: \( n = \frac{\partial \ln \varepsilon_{QSS}}{\partial \ln \sigma} \), where \( \varepsilon_{QSS} \) is the QSS creep rate. The \( \varepsilon_{QSS} \) was determined at \( t_{hold} = 1000 \) s while \( \sigma \) is estimated from \( H \) at \( t_{hold} = 1000 \) s by Tabor’s empirical law, \( \sigma = H/C \), where \( C \) is the constraint factor which is typically ~3 for metals [46]. Note that the value of \( \sigma \) is continuously varying during a constant-load indentation creep test. The
mechanisms related to microstructural activities are predominant. Interfacial diffusion becomes negligible and conventional creep play an important role, whereas for deep indentations the role of GB sliding, GB migration, and GB rotation. Note that these mechanisms are associated with the indenter tip and the sample surface may additionally reduce V*.

Further insight into the mechanism of creep is obtained by estimating the value of the activation volume, V*, which is given by:

\[ V^* = \sqrt{3kT\left(\frac{d\ln V_{SS}}{d\sigma}\right)} \]  

where k is Boltzmann’s constant. It was shown earlier that the value of V* varies by orders of magnitude for different rate-limiting processes [58] with typical values of V* in the ranges from –100b³–1000b³ for dislocation glide in fcc metals down to ~b³ for diffusion either along the GB or through the crystalline lattice [59–61].

The values of V* determined from the slopes of the linear fits of logarithmic \( \epsilon_{QSS} \) vs. linear \( \sigma \) are displayed in Fig. 8. Here, the Burgers vector b for the alloy was calculated as \( b = l \times \sqrt{2/2} \times 2.25 \times 10^{-10} \) m where l is the lattice parameter (~3.60 Å [14]). For cg HEA, the calculated V* is ~4.6b³ which is smaller than V* for the forest dislocation cutting mechanism in conventional metals [58,59]. It was suggested by Wang et al. [62] for shallow indentations that diffusion along the interface between the indenter tip and the sample surface may additionally play an important role, whereas for deep indentations the role of interfacial diffusion becomes negligible and conventional creep mechanisms related to microstructural activities are predominant. In this regard, the smaller-than-typical value of V* for cg HEA may indicate that interfacial diffusion continues to play a role and thus reduces V* while the main governing mechanism is dislocation creep.

In Fig. 8, the V* for nc HEAs is determined as ~0.8b³, which means that the predominant creep mechanism of nc HEAs may be diffusion creep, although there are small primary creep stages (see Fig. 6) that are barely observed in the high-temperature diffusion creep curves. In this regime and for a given \( \sigma \), the steady-state creep rate \( \dot{\epsilon}_{SS} \) is the sum of the creep rate by lattice diffusion, \( \dot{\epsilon}_{QSS} \), and by GB diffusion \( \dot{\epsilon}_{SS,GB} \).

Since \( \dot{\epsilon}_{QSS,GB} \) is negligibly small vis-à-vis \( \dot{\epsilon}_{SS,GB} \), the diffusion creep deformation of nc materials is mainly governed by GB diffusion and its related deformation mechanisms such as Coble creep, GB sliding, GB migration, and GB rotation. Note that these V*

\[ \dot{\epsilon}_{SS} = \dot{\epsilon}_{QSS,GB} = \frac{50b^4}{kT}D_{GB} \]  

where k is Boltzmann constant, T is the absolute temperature, and D_{GB} is the grain boundary diffusivity that is given as an Arrhenius-type equation:

\[ D_{GB} = D_{0,GB}\exp\left(-\frac{Q_{GB}}{RT}\right) \]  

Here, \( D_{0,GB} \) is the pre-exponential factor, R is the gas constant, and Q_{GB} is the activation energy for GB diffusion. As mentioned in the introduction section, SPD processed ultrafine-grained (ufg) metals are known to have a large volume of non-equilibrium GBs which contain a high concentration of extrinsic dislocations [65] giving a larger excess free energy, and hence may exhibit enhanced diffusivities [27–29]. In a recent study [28], the values of \( D_{SS,GB} \) and Q_{GB} for SPD processed ufg Ni were experimentally determined as 1.2 × 10⁻⁸ m²/s and 67 kJ/mol, respectively. By putting these values and \( T = 298 \) K and \( d = 33 \) nm [28] into Eqs. (5) and (6), the theoretical \( \sigma \) dependence on \( \dot{\epsilon}_{SS} \) of nc Ni can be estimated and this is represented by the dashed black line in Fig. 7. As seen, the experimentally obtained \( \dot{\epsilon}_{QSS,SS} \) of nc HEAs is about four or five orders of magnitude smaller than the theoretical \( \dot{\epsilon}_{SS} \). This implies that nc HEAs may have much higher resistance to creep deformation which is consistent with the well-known sluggish diffusion in HEAs.

Fig. 8. Logarithmic strain rate vs. linear stress relation to estimate the activation volume V* for creep.

4.2. Sluggish diffusion effect on creep behavior

As discussed above, the creep deformation in nc HEAs may be primarily governed by GB diffusion and related phenomena. Distinct characteristics of HEAs such as sluggish diffusion leads to the expectation that creep properties of these fcc nc HEAs are different from those of conventional fcc nc metals. Thus, it is constructive to make a direct comparison. A constitutive equation for diffusion creep deformation in nc materials is given as [64]:

\[ \dot{\epsilon}_{SS} = \dot{\epsilon}_{QSS,GB} = \frac{50b^4}{kT}D_{GB} \]  

where k is Boltzmann constant, T is the absolute temperature, and D_{GB} is the grain boundary diffusivity that is given as an Arrhenius-type equation:

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Here, D_{0,GB} is the pre-exponential factor, R is the gas constant, and Q_{GB} is the activation energy for GB diffusion. As mentioned in the introduction section, SPD processed ultrafine-grained (ufg) metals are known to have a large volume of non-equilibrium GBs which contain a high concentration of extrinsic dislocations [65] giving a larger excess free energy, and hence may exhibit enhanced diffusivities [27–29]. In a recent study [28], the values of D_{SS,GB} and Q_{GB} for SPD processed ufg Ni were experimentally determined as 1.2 × 10⁻⁸ m²/s and 67 kJ/mol, respectively. By putting these values and T = 298 K and d = 33 nm [28] into Eqs. (5) and (6), the theoretical \( \sigma \) dependence on \( \dot{\epsilon}_{SS} \) of nc Ni can be estimated and this is represented by the dashed black line in Fig. 7. As seen, the experimentally obtained \( \dot{\epsilon}_{QSS,SS} \) of nc HEAs is about four or five orders of magnitude smaller than the theoretical \( \dot{\epsilon}_{SS} \). This implies that nc HEAs may have much higher resistance to creep deformation which is consistent with the well-known sluggish diffusion in HEAs.
this effect, i.e. $\Delta Q_{GB}$. Since it is difficult to calculate $\Delta Q_{GB}$ in consideration of the sluggish diffusion in the lattice, it is necessary to adopt an indirect approach by using the ratio of $Q_{GB}$ to $Q_i$ where $Q_i$ is the activation energy for the lattice diffusion. Brown and Ashby [66] reported that for fcc metals (such as Ni, Cu, Pb, Au, β-Co, and γ-Fe), the values of $Q_{GB}/Q_i$ are almost constant and close to ~0.6. From this, we calculate $\Delta Q_i$ by sluggish diffusion first and then estimate $\Delta Q_{GB}$ by $-0.6\Delta Q_i$.

Recently, Chang et al. [37] suggested that the three major factors determining $\Delta Q_i$ in multi-component alloys including HEAs are the strain energy of lattice distortion, the packing density of atoms, and the cohesive energy of atoms which can be re-described as

$$\Delta Q_i = (\Delta U_{\text{strain}} + \Delta H_{\text{mix}}) \frac{S_m}{S}$$

(6)

Here, $\Delta U_{\text{strain}}$ is the lattice distortion strain energy, $\Delta H_{\text{mix}}$ is the enthalpy of mixing which corresponds to the change in cohesive energy of the atoms, and $S_m$ and $S$ are the packing densities of a multi-component alloy and a unitary alloy, respectively. The $S_m$ normalized by $S$ in Eq. (6) indicates the extent of difficulty since the diffusion becomes more difficult in a solid having higher packing density [37]. Since it is not feasible to simply define the solvent atoms versus the solute atoms in equiatomic HEAs and thus Eshelby’s elasticity approach [67] cannot be used directly to estimate the value of $\Delta U_{\text{strain}}$, Ye et al. [68] proposed a geometric approach in which the average lattice constant of the alloy is linked to a few critical geometric variables such as atomic size, atomic fraction, and packing density. Using the geometric approach [68], the $\Delta U_{\text{strain}}$ stored in HEAs can be expressed as:

$$\Delta U_{\text{strain}} = \frac{9}{2} K \Omega_{\text{tot}} u_e$$

(7)

where $K$ and $\Omega_{\text{tot}}$ are the average bulk modulus and the total atomic volume of the alloy, respectively, and $u_e$ is the dimensionless elastic energy storage.

For the HEA examined in this study, the $u_e$ of Eq. (7) is 9.67 × 10^{-4} [68] and the bulk modulus $K$ and atomic volume $\Omega$ of each constituent element [69] are listed in Table 1. The $\Delta H_{\text{mix}}$ of Eq. (6) is determined as:

$$\Delta H_{\text{mix}} = 4 \sum_{i=1}^{n} \Delta H_{\text{mix}}^{ij} X_i X_j$$

(8)

where $X_i$ is the molar ratio of the $i$th element and $\Delta H_{\text{mix}}^{ij}$ is the enthalpy of mixing between the $i$th and $j$th elements [70]. Table 2 summarizes the values of $\Delta H_{\text{mix}}^{ij}$ for each combination of constituent elements in the examined HEA. Since the change in packing density is already considered in the geometric model, Eq. (6) can be modified to

$$\Delta Q_i = \Delta U_{\text{strain}} + \Delta H_{\text{mix}} \frac{S_m}{S}$$

(9)

According to Eqs. (8) and (9), $\Delta U_{\text{strain}}$ and $\Delta H_{\text{mix}}$ of the CoCr-FeMnNi HEA can be determined as ~34.4 and ~4.2 kJ/mol, respectively. Then, with $S_m = 0.802$ for the examined HEA [68] and $S = 0.74$ for an ideal fcc lattice, $\Delta Q_i$ is finally estimated as ~30 kJ/mol by Eq. (9). Recently, Tsai et al. [36] empirically investigated $\Delta Q_i$ of each constituent element in the CoCrFeMnNi system and reported that the values are in the range of 18 – 32 kJ/mol. This implies that using Eq. (9) for estimating the value of $\Delta Q_i$ is a reasonable approach. From this, $\Delta Q_{GB}$ by sluggish diffusion was estimated as 0.6$\Delta Q_i$ to give ~17 kJ/mol.

Since there is no principal element in this HEA, the slowest diffusing element that is, Ni, is expected to be rate controlling in diffusion-related deformation [3,4,71]. Therefore, it is reasonable to estimate the theoretical $\xi_{SS}$ for the diffusion creep mechanism of nc HEA on the basis of the diffusion-related parameters of Ni. The only difference is that $Q_{GB}$ of Eq. (5) is no longer $Q_{GB}$ for Ni (without the sluggish diffusion effect) but rather it is the sum of $Q_{GB}$ for Ni (~67 kJ/mol for SPD processed ufg Ni [28]) and $\Delta Q_{GB}$ by the sluggish diffusion effect calculated above (~17 kJ/mol) to thereby give ~84 kJ/mol. Putting this value and $T = 298$ K and $d = 33$ nm into Eqs. (5) and (6) gives the theoretical values for the $\xi_{SS}$ vs. $\sigma$ of nc HEA, which are displayed as a red dotted line in Fig. 7. As shown in the figure, the “theoretical” relation of $\xi_{SS}$ vs. $\sigma$ for the diffusion creep of nc HEA is in reasonable agreement with the experimental results. This implies that the much smaller $\xi_{SS}$ in nc HEA vis-à-vis that of nc Ni may be due to the change in $Q_{GB}$ induced by the sluggish diffusion. The observed small discrepancy between experimental and theoretical results for nc HEAs may be associated with the assumptions inherent in the analysis. For example, $\bar{e}_i$ is converted to $\bar{e}_s$ by the empirical relation $\bar{e}_s \sim 0.01 \bar{e}_i$ based on a study of nc Ni [54] but this may not be valid for other nc materials and also it may vary with the loading conditions [54,72,73].

To summarize, the above results lead to two important characteristics in creep behavior of nc HEAs. First, the room temperature creep of nc HEA is predominantly controlled by GB diffusion. Second, nc HEA exhibits much higher creep resistance as compared to conventional fcc nc metal due mainly to sluggish diffusion. It is noteworthy that although there can be an inevitable difference in diffusion creep results between experiments and theoretical predictions, the above scenario still holds valid because it was shown that the experimental data for diffusion creep support the theoretical model to within a factor of (at most) 4 [74].

### 4.3. Merits of the spherical indentation creep tests

We performed the creep experiments in this study using a spherical indenter whereas most of the nanoindentation experiments—including indentation creep tests—are conducted with a three-sided pyramidal indenter such as a Berkovich tip [42,74–77]. This is because, some issues related to the sharp tip geometry arise in the latter [43,44]. For example, both the characteristic indentation strain and stress underneath a given sharp tip are unique and independent of $t_{\text{creep}}$ because of the geometrical self-similarity of the indenter, which makes it virtually impossible to define the change in strain rate as a function of stress.

To demonstrate this, we investigated the creep exponent $n$ of the nc HEA through typical constant-load sharp indentation creep
tests using a Berkovich indenter. For sharp indentation, $i_t$ is given as $(dh/dt)h^{-1}$ in which the displacement rate $(dh/dt)$ is typically calculated by fitting the $h_{\text{creep}} - h_{\text{hold}}$ curve according to an empirical fitting equation:

$$h(t) = h_0 + A(t_{\text{hold}})^n + Bt_{\text{hold}}$$

(10)

where $A$, $B$, and $k$ are fitting constants. Then, $i_t$ can be converted to $i_u$ by $i_u \sim 0.01i_t$ [54]. The continuous change in the stress during the holding period at $P_{\text{max}}$ was estimated as $H/C$ where $H$ was roughly calculated as $P_{\text{max}}(24.5h^3)$ [79,80] and C-3. Fig. 9 provides representative examples of the data obtained from the Berkovich indentation creep tests made at three different $P_{\text{max}}$ (10, 50 and 100 mN). Similar to the Berkovich creep indentation data in the literature [43,75,76], somewhat implausible behavior can be identified in the figure; i.e., first, the estimated $n$ is very high and second, it increases with $P_{\text{max}}$. $n$ is $14.34 \pm 6.24$ for 10 mN, $18.34 \pm 8.52$ for 50 mN, $34.27 \pm 10.68$ for 100 mN. Considering the fact that $H$ at the onset of creep exhibits a clear trend of indentation size effect (ISE), it appears that $n$ increases with reducing $H$. This trend cannot be explained by classical creep theory in conventional metals where a higher $\sigma$ regime corresponds to higher $n$. Thus, $n$ values of power-law breakdown regime (highest $\sigma$ regime) are higher than those of power-law creep regime (intermediate $\sigma$ regime) and the values are the lowest for the low $\sigma$ regime (diffusion creep or Harper-Dorn creep) [81]. These results confirm that the spherical nanoindentation creep tests adopted here may produce more reliable creep data than the sharp indentation tests that are typically used, at least for the nc HEA tested in this study.

5. Conclusions

In the present study, the nanoscale creep behavior of nc and cg CoCrFeMnNi HEAs was systematically investigated in nanoindentation creep experiments with a spherical tip. The major results of this investigation are as follows.

1. The nc HEAs were successfully synthesized through HPT, which leads to a significant grain refinement after 2 turns and gives a major increase in hardness.

2. Nanoindentation creep experiments reveal that both nc and cg HEAs undergo creep at room temperature. The creep displacement and strain rate of HEAs were increased with the applied strain at the onset of creep.

3. Both the creep stress exponent, $n$, estimated from the quasi-steady-state strain rate and stress and the activation volume $V^*$ suggest that the predominant time-dependent deformation mechanism shifts from dislocation mediated in cg HEA to GB diffusion and its related phenomena in nc HEAs.

4. A theoretical estimate of the creep rate in nc HEA and its comparison with that in conventional nc Ni suggests that creep resistance of nc HEA is significantly enhanced due to sluggish diffusion in HEAs.

5. A comparison of the creep data obtained with spherical and Berkovich tips shows that the former is more appropriate for investigating the creep behavior.

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